Greedy Algorithms: Review

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Main Ingredients

- Safe choice
- Prove safety
- Solve subproblem
- Estimate running time

Safe Choices

Put max digit first

- Choose patient with min treatment time
- Cover leftmost point
- Take item with maximum value per unit of weight

Optimization

- Assume everything is somehow sorted
- Which sort order is convenient?
- Greedy move can be faster after sorting

Safe choice

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Safe choice

- A choice is called safe if there is an optimal solution consistent with this first choice
- Not all first choices are safe
- Greedy choices are often unsafe

Problem

greedy choice

Problem ·

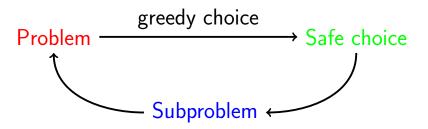
Make a greedy choice

Problem — Safe choice

Make a greedy choice Prove that it is a safe choice

$\begin{array}{c} \mbox{General Strategy} \\ \mbox{Problem} & \xrightarrow{\mbox{greedy choice}} & \mbox{Subproblem} & \leftarrow & \m$

- Make a greedy choice
- Prove that it is a safe choice
- Reduce to a subproblem



- Make a greedy choice
- Prove that it is a safe choice
- Reduce to a subproblem
- Solve the subproblem